1. How does one find the area under a curve f(x) on an interval [a, b] using antiderivatives?

If f(x) has antiderivative F(x), the the area under f(x) on [a, b] is F(b) - F(a).

2. How can you compute the area between two curves f(x) and g(x) on an interval [a, b]?

The area between two curves f(x) and g(x) on the interval [a, b] can be thought of as the area under f(x) minus the area under g(x) on the interval [a, b], which is thus give by

$$\int_a^b f(x)dx - \int_a^b g(x)dx = \int_a^b f(x) - g(x)\,dx$$