

Math 2215 - Calculus 1

Quiz #15 - 2011.05.02

Solutions

1. Compute the following derivatives:

$$(a) \frac{d}{dx} \left[\sin^2(x^2) - \frac{1}{x} + 3 \right]$$

$$\begin{aligned} \frac{d}{dx} \left[\sin^2(x^2) - \frac{1}{x} + 3 \right] &= 2 \sin(x^2) \left[\frac{d}{dx} \sin(x^2) \right] + \frac{1}{x^2} \\ &= 2 \sin(x^2) \left[\cos(x^2) \frac{d}{dx} x^2 \right] + \frac{1}{x^2} \\ &= 2 \sin(x^2) [\cos(x^2) 2x] + \frac{1}{x^2} \end{aligned}$$

$$(b) \frac{d}{dz} [\cos(z^2 f(z))]$$

$$\begin{aligned} \frac{d}{dz} [\cos(z^2 f(z))] &= -\sin(z^2 f(z)) \frac{d}{dz} [z^2 f(z)] \\ &= -\sin(z^2 f(z)) [2z f(z) + z^2 f'(z)] \end{aligned}$$

2. Simplify the expression $48/2(9 + 3)$

$$\begin{aligned} 48/2(9 + 3) &= (48/2) 12 \\ &= 24 \cdot 12 \\ &= 288 \end{aligned}$$