Math 2283 - Introduction to Logic

Quiz #8 - 2010.10.01 Solutions

Recall, if you will, that we were able to define the relation of a class K being a *subclass* of the class L ($K \subset L$) in terms of elements of the universe of discourse:

$$K \subset L \leftrightarrow \underset{x}{A} (x \in K \to x \in L)$$

Let us use the symbol \diamondsuit to represent the relation of being *disjoint*. Construct a definition of the classes K and L being disjoint $(K \diamondsuit L)$ in terms of the elements of the universe of discourse:

$$K \diamondsuit L \leftrightarrow \underset{x}{A} \Big(\sim \big[x \in K \land x \in L \big] \Big)$$

 $\leftrightarrow \underset{x}{A} \Big((\sim x \in K) \lor (\sim x \in L) \Big)$