## Math 2215 - Calculus 1 Quiz #19 - 2017.11.29 Solutions

Express the volume of the region bounded by  $P(x) = 3x^2 - 5x - 2$  and  $Q(x) = 2x^2 - 6x$  revolved around the line y = -5 as an integral. You do not have to evaluate the integral.

First, we set P(x) = Q(x), which gives  $x^2 + x - 2 = 0$ , which can be factored as (x - 1)(x + 2). So the interval on the x-axis over which we have an area to revolve is [-2, 1]. Since P(x) and Q(x) are both parabolas opening upwards, we need to figure out which one is on top. Since x = 0 is in the interval in question, we will use it as a test point: P(0) = -2 and Q(0) = 0. Thus  $P(x) \le Q(x)$  on the interval [-2, 1]. If we use slices  $\Delta x$ , then we would have a washer whose outer radius is  $r_o(x) = Q(x) - (-5) = 2x^2 - 6x + 5$  and whose inner radius is  $r_i(x) = P(x) - (-5) = 3x^2 - 5x + 3$ . Setting up the integral, we now have

$$\mathcal{V} = \int_{-2}^{1} \pi \left[ (2x^2 - 6x + 5)^2 - (3x^2 - 5x + 3)^2 \right] dx$$